Peter Eggleton's
binary stellar evolution code
`ev/STARS/TWIN`

SVN version

User manual

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Contents

1 Creating your first run

See also http://www.phys.uu.nl/~glebbeek/starswiki/bin/view.cgi/Main/GetStarted

1.1 Obtaining and updating the code

To get the code:

1. as a tarball and unpack it,

2. (if you have a log-in account in Utrecht) get it from SVN:
   `svn checkout svn+ssh://<user>@venus.phys.uu.nl/home/strknd/glebbeek/svnroot/stars/trunk stars`

3. (if you have an SVN/Apache account at Northwestern) get the source mirror from SVN:
   `svn checkout https://ciera.northwestern.edu/svn/sluys/eggleton-code/ stars`
   This svn repository only contains source files. You must also obtain the data files etc., *e.g.* from a tarball. Unpack the tarball in a different directory and copy the directories `input/` and `run/` to the directory `stars/` (use `cp -pr` for directories).

Updating the code when using a tarball (option 1 above) is the same as removing and reinstalling the code. When using `svn` (options 2,3), simply `cd` into the `stars` directory and type `svn update`. Don't forget to recompile the code after an update (see Sect. 1.2). A simple `svn` "HOWTO" listing the basic commands can be found here:
`http://www.astro.ru.nl/~sluys/index.php?page=Public/svn-howto`

1.2 Compiling the code

1. `cd` into the directory `stars/`. This is the directory that contains the `code` subdirectory.

2. If you're running on a computer cluster, you probably want to link the executable *statically*. To do this, edit the file `CMakeLists.txt` and set the option `WANT_STATIC` to `on`.

3. Configure and compile (starting from the directory `stars/`). Use CMake (type `cmake --version` to see whether CMake is installed):

   (a) `mkdir build && cd build`

   (b) `cmake ..`

   (c) `make`

   (d) `cd -`

   If you updated the code (and `build/` already exists) and compilation doesn't work, you should type `make clean` before step 3b. If the code *still* doesn't compile, do `rm -rf build/` before step 3a. Note that at step 3b, CMake chooses a compiler. To overrule this, execute *e.g.* `FC=gfortran cmake ..` instead. Step 3c may produce some remarks and should produce the binary executable `code/ev`.

4. It is very useful to set the environment variable to the path of the `stars/` directory, *e.g.* `export evpath="/home/user/codes/stars/"`.[1][2] This line should probably go into your ~/.bashrc. Check with `echo $evpath`.

5. It is very useful to put `ev` in your path. You could do *one* of these:

   (a) `PATH=${PATH}:`echo ${evpath}/code`` (to add the directory where ev sits to your path. Again, you should add this to your ~/.bashrc).

   (b) `cp code/ev ~/bin/` (if ~/bin/ is in your path)

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[1] I'm assuming you're using `bash`. If you're using `csh`, replace `export a="b"` with `setenv a "b"` and ~/.bashrc with ~/.cshrc
[2] Some compilers, *e.g.* `gfortran` don't accept ~/ but need *e.g.* `/home/user/`.

1.3   Running the code

1. I assume you're still in the **stars/** directory.

2. `cd run; ls` — This contains number of subdirectories with different example runs. Let's try the second one and copy the contents in order to keep the original:

3. `cp -r 02-single/ test-02 && cd test-02/ && ls` — The directory contains an example `init.dat` and two example `init.run` files. You need one of each to start a run. Let's use `init.run_m4`, which evolves a $4\,M_\odot$ star:

4. `cp init.run_m4 init.run`

5. We're all ready to start the code. The default syntax is:
   `<path>/ev <output-file base name> <metallicity> <stars directory>`
   and could be *e.g.*:
   `~/codes/stars/code/ev star 02 ~/codes/stars/`
   which is a little annoying, since your code directory is probably not going to move around your hard disc a lot. Hence step 5 in section 1.2, which allows us to remove the path from the **ev** command and step 4 with which we can leave out the last command-line option altogether. Using those steps thus reduces things to:
   `ev star 02`
   The remaining options mean that all my output files will be called `star.*` and that I want to use solar metallicity (02 means $Z = 0.02$, $Z = 0.001$ would reduce to 001, etc. In fact, $Z = 0.02$ is the default option, so I could leave it out and run my first model as:
   `ev star`

1.4   Stopping the code

To terminate a running model properly, you type `echo 1 > fort.11` in the directory where the code is running. (Presumably, we'll want to replace `fort.11` with a proper file name at some point, to facilitate running and terminating different versions of the code in the same directory independently).

2   Modus operandi

The stellar evolution code `ev` is designed to be a binary-evolution code. However, it can be used to compute the evolution of both single and binary stars, and for binaries, there are several possible modes to use the code in. These modes are set by two parameters in `init.run`: ISB (1 or 2, depending on whether we want to evolve one or two stars) and KTW (1 or 2 for non-simultaneous or non-simultaneous binary mode, respectively).

2.1   Single stars

Since `ev` is a binary-evolution code, single stars are in effect in a binary. Since you don't want to waste your undoubtedly valuable (CPU) time on computing the secondary, we set ISB=1 (single star) and KTW=1 (non-TWIN mode — I'm not sure whether it matters, but it seems a safe way to go).

However, here we only tell the code not to compute a model of the secondary. It will still exist, as a point mass. The important thing is that Roche lobes will still be defined, and it is important to set the initial orbital period (PER, in `init.run`) to a sufficiently high value to make sure your 'single star' will not fill its Roche lobe. In addition, I usually set BMS to twice SM, to make sure you don't end up with a negative secondary mass. Experienced users may want to switch off the equations that govern orbital evolution, mass transfer, etc., in `init.dat`, see Sect. 4.6.

2.2   Binary stars

When computing the evolution of a binary, we can choose whether we want to compute a full model of the secondary, or regard it as a point mass (which can be useful when dealing with WD, NS or BH accretors). If we want to compute a detailed model of the secondary, we can choose between *non-simultaneous evolution*, in which the primary is evolved for KP timesteps, before switching to the secondary to catch up in age with the primary, and *simultaneous evolution* (also known as *TWIN mode*), in which both components are evolved at the same time, and mass transfer is taken into account implicitly (this is necessary if *e.g.* both stars have winds).

2.2.1   Primary + point mass

Evolving a binary with a point mass is essentially similar to single-star mode, except that we will set the binary mass (BMS) and the orbital period (PER) to the values we want, and we make sure that the equations for orbital evolution and mass transfer are being solved, see Sect. 4.6. So we set ISB=1 (evolve one star) and KTW=1 (non-simultaneous mode).

2.2.2   Two components, non-simultaneous

This mode was the original way of computing the evolution of a binary: the primary is evolved for KP timesteps, after which the code switches to the secondary, evolves it to the same age as the primary, and it keeps alternating between the two.

This approximates binary evolution sufficiently well for many cases, but it will not when the secondary has a non-negligible wind, or when the secondary fills it's Roche lobe. In other words, all changes to the orbit are made by the primary and the secondary cannot have any influence on the orbit (since if it would, this would affect the evolution of a Roche-lobe-filling primary, which has already been established in the previous semi-cycle).

During the first semi-cycle, while evolving the primary, data on orbital evolution and mass transfer are stored in `file.io12`, which are then read again during the second semi-cycle, where the secondary is evolved.

In order to use this mode, set ISB=2 (evolve two stars) and KTW=1 (non-simultaneous mode), and make sure you solve equations for mass transfer and orbital evolution (see Sect. 4.6).

2.2.3   Two components, simultaneous (TWIN mode)

TWIN mode was developed by Peter Eggleton as an improvement of the non-simultaneous evolution in the previous section. It allows mass loss and mass transfer from the secondary, and, in particular, contact binaries (at least in principle). Both stars are evolved simultaneously, and mass transfer is solved implicitly.

In order to use TWIN mode, set ISB=2 (evolve two stars) and KTW=2 (simultaneous mode), and make sure you solve all necessary equations (see Sect. 4.6).

2.3 Creating grids in mass, mass ratio and period

This is currently broken, due to the way (output?) files are opened.

Apart from computing the model of a single binary (or one single star), the code can be used to compute grids of models, for ranges of initial primary mass, mass ratio and orbital period.

When you want to compute a grid, the initial binary parameters SM, BMS and PER in init.run must be set to negative values, to ensure that they don't override the grid values.

If you want to compute only one model, make sure KML = KQL = KXL = 1.

See Section 5.2 for more details.

3 IO files

3.1 Input files

`init.dat` Initialisation file. Contains the details of the numerics, equations to solve and physics to include while running a stellar model (unit 22).

`init.run` Run control file. Controls the start and stop conditions for different models in a run. One can loop over M_1, $q \equiv \frac{M1}{M2}$ and P_i. Output from different loops is stored in files with different names or in different directories. The file `file.list` gives an overview of which model is stored where (unit 23).

3.2 Output files

As an example I chose the file name `file.*` for the model files.

`file.out1,2` Main output file, showing what the stars are doing at that moment. These files are useful as 'screen output' (units 1,2).

`file.out` Pruned version of the above two files (unit 9). **To be removed?**

`file.io12` Contains orbital and mass-transfer data from star 1, to be used in star 2 in non-TWIN binary mode (unit 3).

`file.mod` Contains a number of complete stellar-structure output blocks. A block from this file can serve as input for a next model (unit 15).

`file.last1,2` Contains complete structure of last and pre-last model, when lucky, that can serve as input for a next run (units 13,14).

`file.list` Shows the starting time and path of a run and tables the properties of the different models and the file names or directories in which they are stored (unit 50).

`file.log` Shows how the code was terminated, if terminated properly (unit 8).

`file.mas` Creation of helper file to find the proper ZAMS model from `zams.mod` (unit 29?)

`file.plt1,2` Contains stellar-evolution data, one model per line (units 31,32).

`file.mdl1,2` Contains a number of complete stellar-structure models, one mesh point per line (units 33,34).

`file.nucout1,2` Main abundances "screen-output file" **true?** (units 35,36).

`file.nucplt1,2` Contains abundances in stellar-evolution models, one model per line **true?** (units 37,38).

`file.nucmdl1,2` Contains abundances in stellar-structure models, one mesh point per line **true?** (units 39,40).

3.3 Data files

The files below can be found in the `input/` directory of the installation and are used for data input (ZAMS, opacities, etc.):

`zahb*.mod` Input structure model for post-helium-flash models (unit 12)

`zahb.dat` "init.dat" for post-helium-flash models (unit 24?)

`zams.mod` Input structure model for ZAMS models (unit 16)

`zams.mas` Reading of helper file to find the proper ZAMS model from `zams.mod` (unit 19?)

`phys.z*` opacity tables for certain metallicity (unit 20?)

`lt2ubv.dat` Data to compute magnitudes and colours from L, T_{eff} (unit 21?)

`nucdata.dat` Data to compute nuclear reactions (unit 26?)

`mutate.dat` Data to **do something with merger products?** (unit 63)

`COtables_z*` Data to compute opacities (unit 41)

`physinfo.dat` **To do** (unit 42)

`rates.dat` **To do** (unit 43)

`nrates.dat` **To do** (unit 44)

3.4 Temporary files

`fort.11` is used to create stop the code, using the command `echo 1 > fort.11`

3.5 Output file by unit

1	file.out1	2	file.out2
3	file.io12		
8	file.log		
9	file.out		
11	(fort.11)		
12	zahb*.mod		
13	file.last1	14	file.last2
15	file.mod		
16	zams.mod		
19?	zams.mas		
20?	phys.z*		
21?	lt2ubv.dat		
22	init.dat	23	init.run
24?	zahb.dat		
26?	nucdata.dat		
29?	file.mas		
31	file.plt1	32	file.plt2
33	file.mdl1	34	file.mdl2
35	file.nucout1	36	file.nucout2
37	file.nucplt1	38	file.nucplt2
39	file.nucmdl1	40	file.nucmdl2
41	COtables_z*		
42	physinfo.dat		
43	rates.dat	44	nrates.dat
50	file.list		
63	mutate.dat		

4 init.dat

The `init.dat` file contains the parameters that are needed to control the numerical details of the code, the differential equations that need to be solved using which variables and boundary conditions and which physics (nucleosynthesis, rotation, stellar wind, overshooting, et cetera). The new format (post–2005 CVS version) contains one parameter (either scalar or array) per line. If a variable name is used multiple times (on multiple lines), the last entry will be used. This is useful for experimenting with values, while keeping the old ones in the file. If a variable is not mentioned at all, the (hard-coded) default value is used.

Thus, the order of the parameters does not matter, but for reasons of clarity and consistency it is a good practice to keep the order used here.

4.1 Output

KT(1) − (4) also known as KT1, KT2, KT3, KT4:

KT1 Print internal details of every `KT1`-th model to `file.out1,2` and `file.mdl1,2` (20 or 200)

KT2 Print internal details at every `KT2`-th mesh point of the `KT1`-th model (`file.out1,2` only) (1 or 2)

KT3 Print KT3 'pages' of details for every `KT1`-th model to `file.out1,2` (1, 2 or 3)

KT4 Print a five-line summary of every `KT4`-th model to `file.out1,2` and save every `KT4`-th evolution model to `file.plt1,2` (1, 2 or 4)

KT5 Print a one-line summary of each iteration of each model to `file.out1,2`, except for the first KT5 iterations of each model (0 or 2)

KSV an output model is stored in `file.mod` (`fort.15`) after every `KSV`-th timestep in a run, in the form needed as input for a further run. The last model of a run is automatically also stored, in `file.last*` (`fort.13,14`). (5000)

KSX(45) The first 15 integers identify the quantities, such as $\log \rho, L, X(^4\mathrm{He}), \ldots$, which are to be printed in columns on the first 'page' of structure details for every KT1-th model. The next two lots of 15 relate to the optional further 'pages'. See section 13.

4.2 Mesh spacing

KH2 The number of mesh points you want; if this differs from KH the code should interpolate in the given model to produce a new one; but you must also set JCH to ≥ 2 to implement this change (199)

JCH If JCH > 1, the REMESH initialises the model in various ways:

JCH = 1 Does nothing.

JCH = 2 Initialises some new variables, for instance the mass,

JCH = 3 = *(2)* + constructs new mesh spacing by interpolation,

JCH = 4 = *(3)* + initialises composition to uniformity (for ZAMS).

At least in some cases JMX in `init.run` must be 0 if JCH > 1 in order for the first model to converge.

CT(1) − (10) coefficients used in the mesh-spacing function Q:
Q = CT(4)*log(P) + CT(5)*log(P+CT(9)) +
CT(7)*log(T) - CT(7)*log(T + CT(10)) -
CT(3)*log(1 + R^2 / CT(8)) +
log(CT(6) * $Mc^{2/3}$ / (CT(6)*$Mc^{2/3}$ + $M^{2/3}$))

CT(1) Unused (0.00)

CT(2) Used for Luminosity weight (0.00, reasonable values seem to be 0.01-1.0, and perhaps other values)

CT(3) Used for Radius weight, together with CT(8) (0.05)

CT(4) Used for Pressure weight, together with CT(5,10) (0.05)

CT(5) Used for Pressure weight, together with CT(4,10) (0.15)

CT(6) Used for Mass weight (0.02)

CT(7) Used for Temperature weight, together with CT(10) (0.45)

CT(8) Used for Radius weight, together with CT(3) (1.E-4)

CT(9) Used for Pressure weight, together with CT(4,5) (1.E15)

CT(10) Used for Temperature weight, together with CT(7) (2.E4)

use_smooth_remesher Switch for the new "smooth" remesher. See also `start_with_rigid_rotation` in `init.run` (.false.)

relax_loaded_model Switch for the new "smooth" remesher. (.true.)

4.3 Time steps

KN The number of variables that will be used for determining the next time step.

KJN(1)-KJN(40) The first KN of these identify the variables to be used for determining the next time step, see section 14.

CT1 The next timestep cannot (normally) be less than CT1 times present timestep (0.8, 0.9 or 1.0)

CT2 The next timestep cannot be greater than CT2 times present timestep. If both CT1 and CT2 are 1.0, then the timestep is constant, of course (which is useful for constructing a ZAMS by artificial 'mass-gain') – except that if a model fails to converge the timestep will be multiplied by CT3 (1.1, 1.05 or 1.0)

CT3 when the solution package fails to converge, the code retreats to the second-last converged model, and continues with the timestep decreased by the factor CT3. (0.3 or 0.5)

4.4 Convergence

KR1 The maximum number of iterations allowed on the first timestep (20)

KR2 The maximum number of iterations allowed on later timesteps (12) If you want to see output when the code is struggeling to converge a model, make sure `KR2 > KT5`.

climit Limit changes in variables during iterations (1.0d-1)

use_quadratic_predictions Normally, the code uses linear extrapolation to predict values for the first iteration on the next timestep. Set this switch to .true. to use quadratic extrapolation, which can be slightly more accurate. (.false.)

use_fudge_control (**obsolete**, present for backward compatibility) Used to switch certain "fudges" on and off, as needed. Now unused. (.true.)

allow_extension (**unused**, present for backward compatibility) Allow the code to do a few extra iterations if it is close to converging when it runs out of iterations. A better approach is to set a convergence window. (.false.)

allow_underrelaxation Allow the code to suppress the diffusion terms in the composition equations and then switch them on slowly as the code iterates. (.false.)

allow_overrelaxation Allow the code to magnify the diffusion terms in the composition equations and then relax them to their normal value as the code iterates. (.false.)

allow_egenrelaxation Allow the code to fall back to the energy generation rate from the previous timestep and then smoothly transition to its current value as the code iterates. (.false.)

allow_mdotrelaxation Allow the code to suppress mass loss from stellar winds or RLOF and switch it on smoothly as the code iterates. (.false.)

allow_avmurelaxation Together with use_previous_mu determines whether the current or the previous value of the mean molecular weight should be used to estimate the effect of thermohaline mixing. Normally best left alone. (.false.)

use_previous_mu Use the previous value of the molecular weight rather than the current value when calculating the effect of thermohaline mixing (for numerical stability reasons). (.true.)

off_centre_weight Used to scale the weighting of terms in the difference equations. A large value means that the weighting is always central, a smaller value means that the weighting moves off-centre for mesh points where the timestep becomes of the order of the thermal conduction time. See Sugimoto (1970) for details. (1.0d16)

4.5   Accuracy

EP(1) − (3) also known as `EPS`, `DEL`, `DH0`. They determine how the code behaves when the mean modulus change in `DH` in the latest iteration equals `ERR` (see Writeup, section 1.6):

EPS The accuracy to which SOLVER is required to solve the equations; if `ERR` < `EPS`, the model has converged. (10^{-6})

wanted_eps The desired accuracy. The solver will aim for an accuracy of `wanted_eps` < `ERR` < `EPS`. This has no effect if `wanted_eps` ≤ `EPS`. (1.0d-8)

DEL If `ERR` > `EPS`, the corrections applied to `DH` are reduced by the factor `DEL/ERR`. (10^{-2})

DH0 Variation in `H` to compute numerical derivatives. (10^{-7})

CDC(1) − (5): CDD is the mean increment, r.m.s.-wise, that you would like in one timestep. Different evolutionary phases have different CDD's (identified here by name rather than by number):

   cdc_ms: CDD = cdc_ms, between ZAMS and core hydrogen 0.04 (corresponding to the beginning of the hook in stars above ∼ 1.2M$_\odot$). (0.04 or 0.01)

   cdc_ems: CDD = cdc_ms * cdc_ems, between the beginning of the hook and hydrogen exhaustion. The purpose is to reduce the timestep so that the hook is properly resolved. (0.15 or 1.0)

   cdc_hg: CDD = cdc_ms * cdc_hg, between core hydrogen exhaustion and the base of the giant branch. The intention is to increase the timestep during the Hertzsprung gap. (3.0 or 1.0)

   cdc_1dup: CDD = cdc_ms*cdc_1dup, during first dredgeup (1DUP) on the giant branch. (0.10 or 1.0)

   cdc_hec: CDD = cdc_ms*cdc_hec, for evolution during core He burning. (0.0625 or 0.25)

   cdc_hes: CDD = cdc_ms*cdc_hes, for further evolution until the He shell nearly catches up with the H shell. (0.25 or 1.0)

   cdc_dblsh: CDD = cdc_ms*cdc_dblsh, for double-shell-burning. The intention is to either make the timestep large and skip over the thermal pulsing phase (if ≥ 1), or to cut back the timestep and resolve the thermal pulses (if < 1). (1.0 or 4.0)

   cdc_rlof: CDD = CDD*cdc_rlof, to reduce the timestep if the system is moving closer to Roche lobe overflow (RLOF). The criterion is that the star is close to filling its Roche lobe and expanding. (0.05 or 1.0)

   cdc_rlof_reduce: CDD = CDD*cdc_rlof_reduce, to keep the timestep smaller while the system detaches after RLOF. The criterion is that the star is close to filling its Roche lobe and shrinking. (0.25 or 1.0)

4.6   Equations, variables and boundary conditions

See also Writeup, section 1.5

KE1, KE2 The number of first and second order difference equations respectively

KE3 Subset of KE1 that involves 3 rather than 2 adjacent mesh points (not yet used, keep 0)

KBC The number of boundary conditions

KEV The number of eigenvalues

KFN The number of 'intermediate functions'

JH1 − JH3 Used for debugging purposes

See also Writeup, section 1.5

kp_var Determines which and in which order the independent variables are used (max 40 integers); a.k.a. `id(11:50)`, `ig(11:50)` in *e.g.* `solver()`.

kp_eqn Determines which and in which order the difference equations are used (max 40 integers); a.k.a. `id(51:90)`, `ig(51:90)` in *e.g.* `solver()`.

kp_bc Determines which in which order the boundary conditions are used (max 40 integers); a.k.a. `id(91:130)`, `ig(91:130)` in *e.g.* `solver()`.

The same contents as lines 5-11, not currently used. See the end of section 1.5 of Writeup.

4.7 Equation of state

KCL(1) − (7) also known as KCL, KION, KAM, KOP, KCC, KNUC, KCN:

KCL Unity includes the Coulomb correction to pressure etc; zero suppresses it. (1)

KION EoS does the ionisation of the first KION elements in the list H, He, C, N, O, Ne, Mg, Si, Fe. No other elements are included. KION = 5 is about optimal. Do not try 9. (5)

KOP If unity, code should use spline interpolation in tables of opacity; if zero, simple bi-linear interpolation (1)

KCN If 0, gives standard nuclear network. If 1, gives a CNO-equilibrium fudge for ZAMS models: see FUNCS1 (0)

eos_include_pairproduction Should the equation-of-state include the effects of pair production? This is only important in the very late burning stages of very massive stars. Positrons are only calculated if their degeneracy parameter $\geq$ -15.0 — otherwise they are negligible anyway. (.false.)

4.8 Nucleosynthesis

CH value for initialising $X(^1\text{H})$ as a fraction of the *total composition*; only used for ZAMS models, with JCH = 4. The default value, CH = −1, tells the code to use the value provided with the ZAMS model. For some (lower?) metallicities and some initial masses ($M \sim 0.8\,M_\odot$?) the ZAMS model may not converge. In such a case setting ML1 to the nearest value for which the ZAMS model converges, and SM to the desired mass (in `init.run`) may help out. (-1.0)

CC, CN, CO, CNE, CMG, CSI, CFE values for initialising $X(^{12}\text{C})$, ... $X(^{56}\text{Fe})$, as fractions of the *total metallicity* Z (= CZS in `input/phys.z*` (`fort.20`)); only used for ZAMS models, with JCH = 4. (0.176, 0.052, 0.502, 0.092, 0.034, 0.072, 0.072)

kr_nucsyn Number of allowed iterations for the nucleosynthesis code (60)

4.9 Rotation

See also `start_with_rigid_rotation` in `init.run`.

rigid_rotation Use rigid rotation, or differential rotation? (.true.)

4.10 Stellar structure

KTH(1) − (4), *alias* KTH − KZ:

KTH ϵ_{th} = KTH * (T DS/Dt); so you can ignore T DS/Dt if you want (1 or 0)

KX D$X(^1\text{H})$/Dt = KX * (burning rate of ^1H); so you can ignore the composition change while keeping the energy production (1 or 0)

KY The same, for ^4He (1 or 0)

KZ The same, for ^{12}C and ^{16}O (1 or 0)

CALP The mixing-length ratio (2.0)

CU Along with COS and CPS, a 'convective overshooting' parameter, see CRD.   (0.1)

COS A convective overshooting parameter for H-burning cores, see CRD. Zero implies no overshooting.   (0.12)

CPS as COS, but for He-burning cores.   (0.12)

CRD The diffusion coefficient σ for convective mixing is taken to be CRD times the 'legitimate' rate from mixing-length theory; except that an approximate multiple of $[\nabla_r - \nabla_a]^{1/3}$ is replaced by the same multiple of $[\nabla_r - \nabla_a + \nabla_{OS}]^2$, where

$$\nabla_{OS} \ \equiv \ \frac{COS}{(2.5 + 20\beta_* + 16\beta_*^2)\,(CU \,\cdot\, \partial \log m / \partial \log P + 1)}, \quad \beta_* \ \equiv \ \frac{P_{\mathrm{rad}}}{P_{\mathrm{gas}}}.$$

The usual CRD is 10^{-2} or 10^{-4}.

CXB Defines the boundary of a core to be at $X(^1\mathrm{H})$ or $X(^4\mathrm{He}) = \mathrm{CXB}$; for printout and envelope binding energy (0.15)

CGR Defines the boundary between a convection zone and a semiconvection zone, for printout purposes only, to be at $\nabla_r - \nabla_a + \nabla_{OS} = \mathrm{CGR}$ (0.001)

CEA A constant energy rate ENC can be added to $\epsilon_{\mathrm{nuc}} + \epsilon_{\mathrm{th}} - \epsilon_\nu$. An increasing ENC can push a star back from the ZAMS to the Hayashi track. CEA and CET determine how ENC changes with time (1.0E2)

CET The equation for the growth of ENC with time is $d\,\mathrm{ENC}/dt = \mathrm{ENC}\times\mathrm{CET}\times(1 - \mathrm{ENC}/\mathrm{CEA})$, so that ENC increases exponentially on the assigned timescale 1/CET (yr), until saturating at ENC $\sim$ CEA. (1.0E-6)

4.11   Mass loss

Individual mass loss recipe switches. These also turn on recipes when smart_mass_loss is used, although that does store its own set of mass loss options (to keep it more modular).

At the surface,

$$\dot{M} = - \ \mathrm{CMT} \cdot \xi \ - \ \mathrm{CMS} \cdot [\log(r/r_{\mathrm{lobe}})]^3 \ + \ \mathrm{CMI} \cdot m \ - \ \mathrm{CMR} \cdot 1.3 \times 10^{-5} \cdot L \cdot m \cdot |E_{\mathrm{BE}}|$$
$$- \ \mathrm{CMJ} \cdot \dot{M}_{\mathrm{JNH}} \ - \ \mathrm{CML} \cdot \zeta(L, r, m, P_{\mathrm{rot}})$$

$([X] \equiv X$ if $X > 0$ and 0 if $X < 0)$

CMT one of two versions of MT by RLOF. CMS & CMT are *alternatives*; set one of them to zero   (0.0, or 1.0D-2–1.0D2 for stars of increasing mass (?))

CMS one of two versions of MT by RLOF. CMS & CMT are *alternatives*; set one to zero   (0.0, or 1.0D0 – 1.0D4). A too-high value can crash the model at the onset of MT.

CMI a constant mass-gain/loss rate, for running up or down the ZAMS, (yr^{-1}) (0.0, $\pm$ 5.0D-9 or $\pm$1.0D-6)

cmi_mode Changes the interpretation of CMI. If cmi_mode = 1, then CMI represents a time scale for exponential mass-gain/loss $(\dot{M} = M \cdot \mathrm{CMI})$. If cmi_mode = 2, then CMI represents a mass-gain/loss rate in solar masses per year.   (1)

4.11.1   Wind mass loss

smart_mass_loss Turn on the smart-mass-loss routine, which picks an appropriate recipe depending on the stellar parameters. This is an alternative for the De Jager rate and replaces it when smart_mass_loss is switched on.   (0.0 (off))

CMR Multiplier for a Reimers-like mass-loss rate: $\dot{M} = \mathrm{CMR} \times M \times \max\left(\frac{1.3 \times 10^{-5}\,L}{U_{\mathrm{bind}}}, \frac{10}{\tau_\nu}\right)$ (0.0 or 0.2–1.0)

CMJ Multiplier for the De Jager mass-loss rate for luminous stars (de Jager et al 1988)   (0.0 or 1.0)

zscaling_mdot Scaling with metallicity applied to De Jager mass-loss rate in `funcs1`   (0.8)

CMV Multiplier for the Vink mass-loss rate

CMK Multiplier for the Kudritzki 2002 mass-loss rate

CMNL Multiplier for the Nugis & Lamers mass-loss rate (for Wolf-Rayet stars)

CMRR Multiplier for the real Reimers mass-loss rate

CMVW Multiplier for the Vasiliadis & Wood (1993ApJ...413..641V) mass-loss rate (superwind for late AGB stars)

CMSC Multiplier for the Schröder & Cuntz mass-loss rate

CMW Multiplier for the Wachter et al. (2002A&A...384..452W) mass-loss rate (superwind for late AGB stars)

CMAL Multiplier for Achmad & Lamers the mass-loss rate (for A supergiants)

cphotontire Switch to include photon tiring   (0.0)

CML A mass-loss rate as obtained from a simplistic dynamo theory   (0.0 or 1.0)

CHL A factor multiplying the rate of ang. mom. loss associated with the rate of mass loss ζ, according to the same dynamo model. (0.0 or 1.0)

cmdotrot_hlw (Multiplier for?) rotationally enhanced mass loss rate by Heger, Langer & Woosely Set at most one of these!

cmdotrot_mm (Multiplier for?) rotationally enhanced mass loss rate by Maeder & Meynet. Set at most one of these!

CTF A factor multiplying an expression for the rate of tidal friction. (0.0 or 0.01)

CLT A coefficient used in the estimation of heat flux between components in contact. It does not really work yet (or does it?).

4.11.2   Mass transfer

cmtel Eddington-limited accretion factor (depends on the stellar parameters)   (0.0d0 or 1.0d0)

cmtwl Angular-momentum limited accretion factor (depends on the stellar parameters)   (0.0d0 or 1.0d0)

ccac Switch for composition accretion   (0.0d0)

cgrs Switch for gravitational settling   (0.0d0)

CPA 'partial accretion': the fraction of one star's wind that is accreted by the other. (0.0)

CBR 'bipolar re-emission': the fraction of material accreted by a star that is ejected in bipolar jets. Needed for CVs, LMXBs. (0.0)

CSU 'spin-up', specifically of the gainer due to accretion. CSU is the specific angular momentum (AM) relative to orbital (OAM), taken out of the orbit by material leaving the L1 point, acquiring AM due to Coriolis force, and landing on the other star - so OAM is converted to gainer's internal AM. Does not seem to work properly... yet. (0.0)

CSD 'spin-down'; the same process also spins down the loser, I suppose, though not by as much. Does not seem to work properly... yet. (0.0)

CDF this is used to convert a step-function into a 'smoothed' step function: see Writeup p.27. (0.01)

CGW A switch to turn gravitational radiation on and off   (0.0 or 1.0)

CSO A switch to turn spin-orbit coupling on and off   (0.0 or 1.0)

CMB A multiplication factor to determine the strength of an alternative magnetic braking law, currently the one by Rappaport, Verbunt & Joss, 1983.   (0.0 – 1.0)

4.12 Mixing

artmix Artificial mixing coefficient [cm^2/s]. Set it to 1.0 to mix the entire star. (0.0d0)

csmc Semi-convection efficiency, after Langer (1991) (4.0d-2)

cdsi Switch for the dynamical shear instability (1.0d0)

cshi Switch for the solberg-hoiland instability (not implemented) (1.0d0)

cssi Switch for the secular shear instability (1.0d0)

cesc Switch for the Eddington-sweet circulation (1.0d0)

cgsf Switch for the goldreich-schubert-fricke instability (1.0d0)

cfmu Weight of mu gradient in rotational instabilities [see Heger's thesis page 36 and Pinsonneault] (5.0d-2)

cfc Ratio of turbulent viscosity over the diffusion coefficient [see Heger's thesis page 35] (3.3d-2)

convection_scheme To do (1)

4.13 Cetera

enc_parachute Emergency energy-generation term, normally set to 0. This cannot be set from the input file. It will be set by `remesh` if there is no nuclear energy generation in the initial model at all. In that case, the first iteration(s) will return LOM = 0.0 throughout the star because the thermal-energy term is initially 0 as well. this is a numerical fudge to remove the resulting singularity. This term will be set to L/M (constant energy generation throughout the star) and will be reduced to 0 by `printb`. (0.0)

5 init.run

The `init.run` file contains parameters that control how to start and stop the run. You have to decide on each of four options, each giving two alternatives. The options are

a) single stars or binary stars

b) new, i.e. starting from scratch (ZAMS), or old, e.g. starting from the end of a previous run.

c) independent evolution ('normal mode'), or *simultaneous* evolution ('TWIN mode'), of the components.

d) a 'one-model' or 'grid' run. A grid means several runs, one after the other (but simultaneous using the massively parallel version, not described here), with the three parameters of primary mass, mass ratio and orbital period being cycled through. One-shot means what it says.

    Not all 16 possibilities make sense: e.g. if you are doing TWIN evolution, you won't want single stars. Many but not all of the remaining possibilities should be viable.

5.1 Mode of operation

ISB, KTW, IP1, IM1, IP2, IM2, KPT, KP

ISB evolve one or two stars. ISB = 1 implies only one star should be computed in detail; ISB = 2 evolves both components of a binary. For *single* stars, you may still use the outer (first) cycle for masses. The inner 2 cycles are automatically set to do only one case each. The mass ratio and the period are of course virtually ignored for single stars, but have to be supplied. The period should be so large that there is no danger of RLOF (see also Sect. 2). (*e.g.* XL = 7.0, meaning a period of $\sim 10^7$ d).

KTW 1 for normal, non-simultaneous operation; 2 for TWIN mode, where both stars are solved *simultaneously*. See Sect. 2 for more detail.

IP1 the number (13 – 16) of the file (fort.13 – fort.16) where the initial model for ∗1 is to be taken from. ZAMS models are on fort.16.

IM1 the sequential number of the model required on fort.IP1. This is computed automatically, from later data, if the ZAMS file fort.16 is used, so that if IP1 is 16, it doesn't matter what value you give for IM1, but you have to give a value.

IP2 as IP1, but for ∗2.

IM2 as IM1, but for ∗2.

KPT the maximum number of timesteps for each component (2000 to 4000 for fairly complete evolution). You may set KPT equal to -1 to indicate that the code should run until one of the termination conditions is met, in other words, the code will not stop when it reaches a predetermined number of timesteps.

KP Do approximately KP of ∗1, then enough of ∗2 to catch up with ∗1, then another $\sim$ KP of ∗1, etc, so that if ∗2 breaks down before ∗1 you don't waste a lot of calculation on ∗1. You will seldom get *exactly* the number of timesteps that you ask for. For single stars, KP is set to KPT automatically.

5.2 Grids of masses and periods

ML1, DML, KML; QL1, DQL, KQL; XL1, DXL, KXL

These three lines contain parameters for 3 nested loops (mass, mass ratio, and initial period) to be run through. Each loop has: starting value; increment; number of cases (1 more than the number of increments).

- The first (outer) loop is: $\log_{10}$ (mass, solar units), starting at ML1, increasing by steps of DML to ML1 + (KML − 1) . DML

- The second loop is: $\log_{10}$ (mass ratio in sense {larger/smaller}), starting at QL1, increasing by steps of DQL to QL1 + (KQL − 1) . DQL

- The third (inner) loop is: X $\equiv \log_{10}$(orbital period /period necessary for ∗1 to fill its Roche lobe when still on the ZAMS), starting at XL1, increasing by steps of DXL to XL1 + (KXL − 1) . DXL.

- If you want to compute only one model (single or binary), set KML = KQL = KXL = 1.

When a grid is computed, the initial binary parameters SM, BMS and PER must be set to negative values, to ensure that they don't override the grid values.

5.3 Rotation and eccentricity

ROT, KR, EX

ROT, KR KR = 1: $P_{\rm rot}$ for each star = rotational breakup period * $10^{\rm ROT}$ **PERC: breakup or RLOF at ZAMS?**

   KR = 2: $P_{\rm rot}$ for each star = max(1.05 * rotational breakup period, orbital period * $10^{\rm ROT}$) **PERC: breakup or RLOF at ZAMS?**

   KR ≥ 3: set $P_{\rm rot} = P_{\rm orb}$; (almost) synchronous rotation

EX the initial eccentricity.

5.4 Initial binary parameters

SM, DTY, AGE, PER, BMS, ECC, P, ENC, JMX

(a.k.a. AX(1-8), JMX). The AX's are optional replacements for the values of SM, ..., ENC that the code would normally pick up in fort.IP1 from some previous run, or from the ZAMS library (fort.16). JMX similarly is an optional replacement for JMOD. They are only applied if they are non-negative. Thus you can replace only one, or several.

SM Primary mass [$M_\odot$]

DTY Time step [yr]

AGE Model age [yr]

PER Orbital period [d – or fraction of break-up?]

BMS Total binary mass [$M_\odot$]

ECC Orbital eccentricity

P Spin period of the primary [d]

ENC Artificial energy rate, see CEA and CET [?]

JMX New model number (JMOD). Set to -1 to keep unchanged, to 0 to set the mass of a ZAMS model using the loop parameters ML1,QL1 above, ignoring SM (when using IP1,2=16) **True?** and to any positive value to start counting models at that value. For grids looping over primary mass and mass ratio, you *must* set JMX to 0! **In some cases, when restarting an evolved model, you seem to have to set JMX to > 0!**

START_WITH_RIGID_ROTATION

Can be TRUE or FALSE.

5.5 Termination conditions

UC:

The last three lines are a set of 21 criteria (UC(1–21)) to determine when the run is to be ended (e.g. when the age is greater than 2×10^{10} yr), or when some special procedure should be initiated (e.g. the He-flash evasion). You'll have to read the end of printb.f to figure them out completely. In many cases the code is stopped by changing the termination code *JO*.

UC(1-7):

UC(1): (rlf1) Terminate if FLR(=RLF?) (Sect. 9, nr 29) of star 1 exceeds this number ($JO = 4$) (0.1)

UC(2): (age) Terminate if the age of the model in years exceeds this number ($JO = 5$) (2e10)

UC(3): (LCarb) Terminate if $L_C >$ this number ($JO = 6$) (100)

UC(4): (rlf2) Terminate if FLR(=RLF?) (Sect. 9, nr 29) of star 2 exceeds this number ($JO = 7$) (0.2)

UC(5): (LHe) Initiate He-flash evasion if $L_{He} >$ this number, together with UC(6) ($JO = 8$) (1e3, lower for $M_* \approx 2M_\odot$)

UC(6): (rho) Initiate He-flash evasion if $\log \rho_c >$ this value (?), together with UC(5) ($JO = 8$) (5.3)

UC(7): (MCO) Terminate if degenerate CO-core exceeds this mass, together with UC(8) ($JO = 9$) (1.2)

UC(8-14):

UC(8): (rho) Terminate if $\log \rho_c >$ this value (?), together with UC(7) ($JO = 9$) (6.3)

UC(9): (mdot) Terminate if $|\dot{M}| > $ UC(9) $* M_*/\tau_{KH}$ ($JO = 10$) (3e2)

UC(10): (XHe) Change eps (next number) if the core Helium abundance drops below this number (0.15)

UC(11): (eps) If $Y_{core} <$ XHe (previous number), set EPS to this number. Do not use, keep this number 1e-6! (1e-6)

UC(12): (dtmin) Terminate if $\Delta t <$ dtmin (in seconds?) (1e6)

UC(13): (sm8) The total mass the post-He-flash model should get, can also be used manually! (1e3)

UC(14): (vmh8) The He-core mass he post-He-flash model should get, can also be used manually! (1e3)

UC(15-21):

UC(15): (XH) If > 0: terminate if the core H-abundance drops below this value, you can e.g. stop at the TAMS ($JO = 51$) (0.0)

UC(16–21): Unused

6   file.mod

This file contains stellar structure output, that can be used as input. The files `file.last1,2` have the same format.

The file consists of one or more blocks, starting with a single line with 13 model properties and followed by a block with one line per mesh point with the independent variables. This block contains 24 columns of which only part is used. Some of them are 'eigenvalues' and have the same value for every mesh point.

6.1   Header

The first line of the file contains the 13 numbers:

1. M_1, the mass of the primary $[M_\odot]$

2. Δt, time step [yr]

3. t, age of the model [yr]

4. P_{orb}, the orbital period [day]

5. BMS, the total binary mass $[M_\odot]$

6. e, the orbital eccentricity

7. P_{rot}, the rotational period [day]

8. enc, artificial energy term [?]

9. kh, the number of mesh points and thus rows in the stellar structure block below

10. kp, the total number of models to calculate

11. $jmod$, the current model number

12. jb, the number of this star in the binary [1 or 2]

13. jin, the number of independent variables and thus columns in the stellar structure block below [24 for non-TWIN, 40 for TWIN]

14. jf, do or do not overwrite overwrite I and ϕ (see below). Just keep it 0. [0 or 2]

6.2 Blocks of stellar structure

Each block contains the contents of the variable H: 24 models for non-TWIN models, and 40 for TWIN models. Columns 1–16 are reserved for the primary, 17–25 for binary parameters and 26–40 have the same content as 1–16, but for the secondary in the TWIN case. In the loop over all meshpoints in `printb`, the variable `Q(1-24)` contains the same data as `H(1-24,I)` (or the corresponding variables for the secondary in a TWIN model) for each mesh point `I`. Each line represents a mesh point, the first one usually the *surface* of the star. The 'eigenvalues' are marked with *(EV)*. The columns are:

1. $\ln f$, a dimensionless quantity closely related to electron degeneracy: for the case where electrons are non-degenerate and non-relativistic, $f \sim 10^8 \rho / T^{1.5}$

2. $\ln T$, logarithmic temperature [K]

3. $X16$, mass abundance fraction of ^{16}O

4. m, mass [10^{33} g]

5. $X1$, mass abundance fraction of ^{1}H

6. C, the gradient of mesh-spacing function $Q(f, T, m, r)$ with respect to mesh point number K *(EV)*.

7. $\ln r$, logarithmic radius [10^{11} cm]

8. L, luminosity. Not logged, because it may be negative [10^{33} erg s^{-1}]

9. $X4$, mass abundance fraction of ^{4}He

10. $X12$, mass abundance fraction of ^{12}C

11. $X20$, mass abundance fraction of ^{20}Ne

12. I, the moment of inertia of the interior material [10^{55} g cm^2]

13. P_{rot}, the rotation period (days) of the star *(EV)*.

14. ϕ - the centrifugal-gravitational potential [erg]

15. ϕ_{s}, the potential at the surface, minus the potential on the L1 surface *(EV)* [erg]

16. $X14$, mass abundance fraction of ^{14}N

17. H_{orb}, the orbital angular momentum *(EV)* [10^{50} gm cm^2 s^{-1}]

18. e, the orbital eccentricity *(EV)*

19. F, the flux of mass towards or away from the other star; a function of depth and zero below L1 [10^{33} g s^{-1}]

20. *<empty>*

21. *<empty>*

22. *<empty>*

23. *<empty>*

24. *<empty>*

25. – 40.: The same as variables 1–16, but for the secondary in case of a TWIN model, otherwise empty (since *jin* (above) equals 24 in that case).

7 file.log

This file contains the exit code with which the Eggleton code terminated. Usually, the file lists an explanation of these codes at the top of the files, but for grids these lines may lack.

-2 Requested mesh too large (`BEGINN`)

-1 No timesteps required (`STAR12`)

0 Finished required timesteps (`STAR12`)

1 Failed; backup, reduce timestep (`SOLVER`)

2 Time step reduced below limit; quit (`BACKUP`)

3 Star 2 evolving beyond last star 1 model (`NEXTDT`)

4 Star 1: stellar radius exceeds Roche-lobe radius by limit (UC(1), `PRINTB`)

5 Age greater than limit (UC(2), `PRINTB`)

6 Carbon burning exceeds limit (UC(3), `PRINTB`)

7 Star 2 radius exceeds Roche-lobe radius by limit (UC(4), `PRINTB`)

8 Close to helium flash (UC(5,6), `PRINTB`)

9 Massive ($> 1.2 M_\odot$), degenerate CO core (UC(7,8), `PRINTB`)

10 $|\dot{M}_1|$ exceeds limit (UC(9), `PRINTB`)

11 Impermissible FDT for star 2 (`NEXTDT`)

12 Time step reduced below limit – hydrogen left in the core; quit (`BACKUP`)

14 Funny composition distribution ($M_\mathrm{H} < M_\mathrm{He}$ or $M_\mathrm{He} < M_\mathrm{CO}$, `PRINTB`)

15 Terminated by hand (`STAR12`)

16 ZAHB model didn't converge (`MAIN`)

17 Nucleosynthesis didn't converge (`BEGINN`)

22 Time step reduced below limit – helium left in the core; quit (`BACKUP`)

32 Time step reduced below limit – carbon left in the core; quit (`BACKUP`)

51 End of MS (core hydrogen abundance below limit) (UC(15), `PRINTB`)

52 Radius exceeds limit (`PRINTB`)

53 Convergence to target model reached minimum (`PRINTB`)

8   file.out{1,2}

Note: this section is about `file.out1` and `file.out2`, not `file.out`!

During a stellar evolution run short summaries of the stellar parameters are written into the files `file.out1` and `file.out2`. It can be useful to watch this file while the code is running for example by typing `tail -f file.out1`. This will show the last 10 lines of the `file.out1` file and refresh when `file.out1` changes (exit with `Ctrl-C`). The files start with a copy of `init.dat`. The rest of the file consists of three different blocks of information:

Stellar snapshots: summaries of the star at a certain model number, *e.g.* its mass, age, central composition, etc.,

Stellar slices: detailed summaries of the interior of the star, *e.g.* P ρ, T, etc., on every mesh point in the star,

Convergence info: information on the convergence of the set of differential equations for each iteration.

How often these blocks of information are printed to the file can be set with the parameters KT1 − KT5 in `init.dat`.

8.1   Stellar snapshots

Line 1:

M: Stellar mass [$M_\odot$]

Porb: Orbital period [days]

xi: Mass transfer rate [$M_\odot$ yr^{-1}]

tn: Nuclear timescale

LH: Luminosity by Hydrogen burning

P(cr):

McHe: Mass of Helium core

CXH: Central H Abundance

CXHe: Central He abundance

CXC: Central C abundance

CXN: Central N abundance

CXO: Central O abundance

CXNe: Central Ne Abundance

CXMg: Central Mg abundance

Cpsi: Central value of the electron degeneracy parameter

Crho: Log Central density

CT: Log Central Temperature

Line 2:

dty: Time step [yr]

Prot: Rotational period [days]

zet: Mass loss rate other than Roche lobe overflow, *e.g.* wind. $[M_\odot \text{ yr}^{-1}]$

tKh: Kelvin-Helmholtz timescale

LHe: Luminosity due to helium burning

RCZ:

McCO: Mass of CO core

TXH: H abundance at $T_{\max}$

TXHe: He abundance at $T_{\max}$

TXC: C abundance at $T_{\max}$

TXN: N abundance at $T_{\max}$

TXO: O abundance at $T_{\max}$

TXNe: Ne abundance at $T_{\max}$

TXMg: Mg abundance at $T_{\max}$

Tpsi: Value of the electron degeneracy parameter at $T_{\max}$

Trho: log $T_{\max}$

TT: log rho at $T_{\max}$

Line 3:

age: Stellar age [yr]

ecc: Orbital eccentricity

mdt: Mass loss $[M_\odot \text{ yr}^{-1}]$

tET: Envelope Turnover timescale of the convective envelope

LCO: Luminosity due to Carbon/Oxygen burning

DRCZ:

McNe: Mass of Neon Core

SXH: Surface abundance of H

SXHe: Surface abundance of He

SXC: Surface abundance of C

SXN: Surface abundance of N

SXO: Surface abundance of O

SXNe: Surface abundance of Ne

SXMg: Surface abundance of Mg

Spsi: Surface value of the electron-degeneracy parameter

Srho: Log Surface density

ST: Log Surface Temperature

Line 4:

cM: Companion Mass $[M_\odot]$

RLF1: Relative Roche-lobe radius $[\log R/R_{\mathrm{rlof}}]$

RLF2: Relative Roche-lobe radius $[\log R/R_{\mathrm{rlof}}]$

DLT:

Lnu: Luminosity due to neutrino losses

RA/R: Alfvén radius $[R_*]$

MH: Total hydrogen mass in the star $[M_\odot]$

conv. bdries: Mass coordinates of convective boundaries (3 pairs)

logR: Log R

logL: log L

Line 5:

Horb: Orbital angular momentum

F1:

DF21:

BE:

Lth: Luminosity from contraction/expansion

Bp: Poloidal component of the magnetic field

MHe: Total helium mass in the star $[M_\odot]$

semiconv. bdries: Mass coordinates of semiconvective boundaries (3 pairs)

k**2: Dimensionless axis of gyration, if moment of inertia is calculated in the code.

8.2 Convergence info

Iter The first integer displays the number of iterations,

Err The logarithm of the total error,

Ferr The residue in the current iteration,

Fac The factor by which corrections are multiplied before being applied. Normally 1.00, but may be smaller if the code has trouble converging.

Then a list of numbers follows, in pairs of an integer and a float (*e.g.* $79 - 9.2$). There is one pair for each independent variable. The integer indicates the mesh point in the star (1 indicates the core) where the largest error for this independent variable occurs and the float indicates the log of the error in that mesh point. In practice this means that $(199 - 9.9)$ is a good thing since $10^{-9.9}$ is a very small error, $(98 - 3.1)$ is worrying and when the floats get to -2.0 or larger something is really wrong. It is usually a good idea to scroll up and look whether earlier blocks exist and, if so, to see whether the same variables are causing the problems there — sometimes one variable starts causing problems and then drags along others.

9 file.plt{1,2}

This file contains stellar evolutionary properties, for one structure model per line. The first line contains the number of columns in the output block. The block currently contains 81 columns, with the following contents:

1. JMAD, Model number

2. t, Age [yr]

3. Δt, time step [yr]

4. M, stellar mass [$M_\odot$]

5. M_{He}, helium core mass [$M_\odot$]

6. M_{CO}, carbon-oxygen core mass [$M_\odot$]

7. M_{ONe}, oxygen-neon core mass [$M_\odot$]

8. $\log R$, stellar radius [$R_\odot$]

9. $\log L$, stellar luminosity [$L_\odot$]

10. $\log(T_{\mathrm{eff}})$, effective temperature [K]

11. $\log T_{\mathrm{c}}$, central temperature [K]

12. $\log T_{\mathrm{max}}$, maximum temperature [K]

13. $\log \rho_{\mathrm{c}}$, central density [g cm^{-3}]

14. $\log \rho_{\mathrm{Tmax}}$, density at $T = T_{\mathrm{max}}$ [g cm^{-3}]

15. U_{bind}, binding energy of H envelope [erg/(1 $M_\odot$)] [3]

16. L_{H}, luminosity by hydrogen burning [$L_\odot$]

17. L_{He}, luminosity by helium burning [$L_\odot$]

18. L_{C}, luminosity by carbon burning [$L_\odot$]

19. L_ν, neutrino luminosity [$L_\odot$]

20. L_{th}, luminosity by release of thermal energy [$L_\odot$]

21. P_{rot}, rotational period [days]

22. VK2, $K^2 \equiv \frac{I}{M R^2}$, with I the moment of inertia

23. R_{cz}, Depth (?) of convective envelope [R_*]

24. dR_{cz}, Thickness (?) of convective envelope [R_*]

25. TET, Convective turnover timescale

26. RAF, Alfvén radius

27. BP, poloidal magnetic field

28. P_{orb}, orbital period [days]

29. FLR $= {}^e\log(R_*/R_{\mathrm{rl}})$, relative Roche Lobe Radius, also called RLF

30. F1, $\sim \Phi_{\mathrm{surf}} - \Phi_{\mathrm{L1}}$ [erg] ?

31. $\dot{M}$, total mass loss [$M_\odot$ yr^{-1}]

---

[3]Multiply with 1.9891×10^{33} to get ergs. The reason for this confusing solution is that values of 10^{40-50} erg don't fit in a single-precision variable, and that the value may be negative so that a log is no option.

32. $\dot{M}_{\mathrm{wind}}$, wind mass loss $[M_\odot\ \mathrm{yr}^{-1}]$

33. $\dot{M}_{\mathrm{mt}}$, mass transfer rate $[M_\odot\ \mathrm{yr}^{-1}]$

34. H_{orb}, orbital angular momentum $[10^{50}\ \mathrm{g\ cm^2\ s^{-1}}]$

35. dH_{orb}/dt, total orbital angular momentum loss rate $[10^{50}\ \mathrm{g\ cm^2\ s^{-2}}]$

36. dH_{gw}/dt, change in H_{orb} due to gravitational waves $[10^{50}\ \mathrm{g\ cm^2\ s^{-2}}]$

37. dH_{wi}/dt, change in H_{orb} due to wind mass loss $[10^{50}\ \mathrm{g\ cm^2\ s^{-2}}]$

38. dH_{so}/dt, change in H_{orb} due to spin-orbit coupling $[10^{50}\ \mathrm{g\ cm^2\ s^{-2}}]$

39. dH_{ml}/dt, change in H_{spin} due to non-conservative mass transfer $[10^{50}\ \mathrm{g\ cm^2\ s^{-2}}]$

40. M_{comp}, companion mass $[M_\odot]$

41. e, orbital ellipticity

42. – 48. Surface abundances of: 42:H, 43:He, 44:C, 45:N, 46:O, 47:Ne, 48:Mg

49. – 55. T_{max} abundances of: 49:H, 50:He, 51:C, 52:N, 53:O, 54:Ne, 55:Mg

56. – 62. Central abundances of: 56:H, 57:He, 58:C, 59:N, 60:O, 61:Ne, 62:Mg

63. – 68. Convection zone boundaries (`mcb`); > 0: beginning, < 0 end of zone (max. 3 sets)

69. – 74. Semi-convection zone boundaries (`msb`); > 0: beginning, < 0 end of zone (max. 3 sets)

75. – 80. Nuclear energy production zone ($\varepsilon_{\mathrm{nuc}} > \varepsilon_{\mathrm{tresh}} \sim 10 L_*/M_*$) boundaries (`mex`); > 0: beginning, < 0 end of zone (max. 3 sets)

81. Q_{conv}, the mass fraction of the convective envelope

82. P_{c}, central pressure [cgs]

83. $P_{\mathrm{rot,c}}$, rotational period in the centre [s] [4]

84. BE_0, binding energy due to gravitational energy $[\mathrm{erg}/(1\ M_\odot)]$ [3]

85. BE_1, binding energy due to internal energy $[\mathrm{erg}/(1\ M_\odot)]$ [3]

86. BE_2, binding energy due to recombination energy $[\mathrm{erg}/(1\ M_\odot)]$ [3]

87. BE_3, binding energy due to H_2 association energy $[\mathrm{erg}/(1\ M_\odot)]$ [3]

88. S_{c}, specific entropy in core $[\mathrm{erg\ g^{-1}\ K^{-1}}]$

89. $S_{T=10^5 K}$, specific entropy in the convective envelope at $T = 10^5 \mathrm{K}$ $[\mathrm{erg\ g^{-1}\ K^{-1}}]$

90. R_{He}, radius of the helium core $[R_\odot]$

91. R_{CO}, radius of the CO core $[R_\odot]$

92. STRMDL, a structure model is stored (1.0) or not (0.0)

---

[4]The latest 2005 version, used at NU, has STRMDL in column 83 and column 89 as its last column.

10 file.mdl{1,2}

The files `file.mdl1` and `file.mdl2` contain stellar-structure output, designed for plotting the stellar interiors. Each file starts with a line of 3 numbers, followed by a number of blocks, each of which contains a stellar-structure model saved during the evolution of the model star. The parameter `KT1` determines how often a structure model is saved. Each block starts with a line with two numbers. The rest of each block contains (typically a few hundred) lines each with (a few tens of) columns.

10.1 Header

The first line of the file contains three parameters:

1. N_{mesh}; number of mesh points in each model (= the number of rows in each block), see the parameter `KH2`.

2. N_{var}; number of output variables (= the number of columns in the blocks)

3. $D_{\text{overshoot}}$ **(= overshoot parameter `COS` ?)**

10.2 Blocks of stellar structure

Each block starts with one line with two values:

1. Model number for the block of output below

2. t, model age [yr]

The first line of each block is followed by an array of data consisting of N_{mesh} rows of N_{var} columns each. Hence, each row is a mesh point in the stellar model (a mass coordinate or radius coordinate). The first row of each block contains data for the *centre* of the star, the last (N_{mesh}-th) row represents its *surface*. In each row, there are N_{var} columns. Each column contains a different physical quantity.

The quantities in the columns are:

1. M, mass coordinate [$M_\odot$]

2. R, radius coordinate [$R_\odot$]

3. P, pressure [dyn cm^{-2}]

4. ρ, density [g cm^{-3}]

5. T, temperature [K]

6. κ, opacity [cm^2 g^{-1}]

7. $\nabla_{\text{ad}} = \left(\frac{\partial \log T}{\partial \log P}\right)_{\text{ad}}$, adiabatic temperature gradient [-]

8. $\nabla_{\text{rad}} - \nabla_{\text{ad}}$, temperature gradient difference [-]

9. – 15. Abundances of: 9: H, 10: He, 11: C, 12: N, 13: O, 14: Ne, 15: Mg

16. L, total luminosity [$L_\odot$]

17. ε_{th}, energy generation due to contraction (can be negative) [erg g^{-1} s^{-1}]

18. ε_{nuc}, energy generation by nuclear reactions [erg g^{-1} s^{-1}]

19. ε_ν, energy generation in neutrinos [erg g^{-1} s^{-1}]

20. S, specific entropy [erg g^{-1} K^{-1}]

21. U_{int}, internal energy [erg g^{-1}]

22. Reaction rate RPP: pp chain, effectively: 2 p $\to \frac{1}{2}$ He4

23. Reaction rate RPC, effectively: C12 + 2 p $\to$ N14

24. Reaction rate RPNG, effectively: N14 + 2 p → O16

25. Reaction rate RPN, effectively: N14 + 2 p → C12 + He4

26. Reaction rate RPO, effectively: O16 + 2 p → N14 + He4

27. Reaction rate RAN, effectively: N14 + $\frac{3}{2}$ He4 → Ne20

28. $C_p \frac{\mathrm{d}S}{\mathrm{d}P}$

29. μ, mean molecular weight [amu]

30. Mixing coefficient for thermohaline mixing (or unused)

31. Mixing coefficient for convective mixing (convective velocity $\times$ mixing length)

32. True temperature gradient: $\frac{\mathrm{d}\log T}{\mathrm{d}\log P}$

33. ω, rotation rate **CHECK**

34. **CHECK:** $d\mu$**?**

35. **CHECK:** $d\omega$**?**

36. **CHECK: Convection + artificial mixing**

37. **CHECK: Thermohaline mixing**

38. **CHECK: Solberg-Hoiland mixing**

39. **CHECK: Dynamical-shear mixing**

40. **CHECK: Secular-shear mixing**

41. **CHECK: Eddington-Sweet mixing**

42. **CHECK: Goldberg-Schubert-Fricke mixing**

11   Creating a ZAMS model

Note that this section is about manual meddeling with models — you don't need this for normal operation of the code, e.g. to change the ZAMS mass of a model, for that see the section init.run. If you want to create a ZAMS series, see the example run 01 in the directory run/01-zams/.

In order to create a (ZAMS) model of certain mass, or to obtain a series of ZAMS models, one can use the RMG mass loss/gain parameter in the init.dat file. This parameter gives a mass loss or mass gain that is proportional to the mass of the star.

The method is as follows:

- Choose an existing input model with a mass close to the desired mass

- Set the parameter CMI to the desired value (usually $\pm 5 \times 10^{-9}$)

- Make sure the time step doesn't change (CT1 = CT2 = 1.00

- Calculate the factor f with which you want to change the mass to get from the model you have to the model you want. (If you have 1.00 $M_\odot$ and want 1.02 $M_\odot$, $f = 1.02$)

- Calculate the approximate number of steps you need to take for a time step size $dt_0 = 10^3$ yr and the CMI above: $N_0 = \frac{\ln f}{\text{CMI } dt_0}$

- Choose a (nice, round, but at least) integer number of steps $N \approx N_0$

- Calculate the true time step for N steps: $dt = \frac{\ln f}{\text{CMI } N}$

- Fill in the values for dt and N in init.run

- Run the model for N steps and check the final mass in file.mod

$$dt = \frac{\ln\left(\frac{M_f}{M_i}\right)}{N \ \ \text{CMI}}$$

The Fortran program makezams.f (see website) is supposed to do all the above.

If all goes well, you'll end up with the mass slightly off. You can give your model the exact mass you want by switching off the wind, put the desired mass in init.run and run another 10 models or so.

If the change in mass is less than expected, you may have chosen your timestep too long, so that the code does not converge, recalculates the model with a smaller timestep and continues with this smaller timestep (since it is not allowed to change).

12 Creating a ZAHB model

In order to create a ZAHB model, for instance because the format of the input files has changed or because you want a different metallicity, you can use the following recipe. Most of the work is actually already done by test run 07. However, or lower metallicities you will need a more massive ZAMS star and it may be harder to get a low-mass ZAHB star.

- Evolve a $2.25 M_\odot$ star until it starts core helium burning. Do not allow the helium to be consumed (KY=0). This is done in run 07a.

- Start mass loss until the star is down to about $0.4 M_\odot$. This step is covered by run 07b.

- Put the starting model and an appropriate init.dat file in `input/zahb<Z>.mod`, where Z is the metallicity (02 for $Z = 0.02$, etc.)

- Test the result for a $1.0 M_\odot$ model (run 03).

- If the code can produce the ZAHB model, but it cannot continue the evolution on the HB (error code 16), the problem may be a too-small desired number of models (see the parameter kp in the first (*i.e.* header) line of the structure model) in `input/zahb<Z>.mod`.

13   Variables in SX and PX

These quantities are calculated in `printb` and stored in the variables `SX` and `PX`. In the loop over all meshpoints, `SX(J, IKK)` is the previous value of `PX(J)`, from the previous mesh point. `IKK` runs from 1 to `NM`, the number of meshpoints, or from the centre to the surface of the star. (In the same loop, the variable `Q(1-24)` contains the values of `H(1-24,I)` for mesh point `I`, see Sect. 6).

1. ψ: degeneracy parameter ?

2. P: Pressure

3. ρ: Mass density

4. T: Temperature

5. κ: Opacity

6. ∇_{ad}: Adiabatic temperature gradient $\left(\frac{\partial \log T}{\partial \log P}\right)_{\mathrm{ad}}$

7. ∇: True temperature gradient $\frac{d \log T}{d \log P}$

8. $\nabla_{\mathrm{rad}} - \nabla_{\mathrm{ad}}$: Difference between the radiative and adiabatic ∇'s

9. M: Mass

10. H^1: Hydrogen abundance

11. He^4: Helium abundance

12. C^{12}: Carbon abundance

13. N^{14}: Nitrogen abundance

14. O^{16}: Oxygen abundance

15. Ne^{20}: Neon abundance

16. Mg^{24}: Magnesium abundance

17. R: Radius

18. L: Luminosity

19. E_{th}: Thermal energy generation rate

20. E_{nuc}: Nuclear energy generation rate

21. E_{ν}: Energy loss rate in neutrinos

22. dM: Shell mass

23. Diffusion coefficient for thermohaline mixing

24. $\frac{n}{(n+1)} = \frac{d \log \rho}{d \log P}$: Homology invar.

25. $U_{\mathrm{hom}} = \frac{d \log R}{d \log P}$: Homology invar.

26. $V_{\mathrm{hom}} = \frac{d \log M}{d \log P}$: Homology invar.

27. U: Internal energy

28. S: Entropy

29. L/L_{edd}: Luminosity relative to Eddington

30. $w_{\mathrm{conv}} \times l$, w_{conv}: convective velocity, l: mixing length

31. μ: Mean molecular weight

32. wt: ?

33. ν_e: $\frac{1}{\mu}$: per free electron

34. $\nu_{e,0}$: $\frac{1}{\mu_0}$: per all electrons

35. w_{conv}: convective velocity

36. M.I.: Moment of Inertia

37. ϕ: centrifugal-gravitational potential

38. F_m: Mass flux towards or away from the other star

39. DGOS: $\nabla_r - \nabla_a + \nabla_{OS}$ modified Schwarzschild criterion: if > 0: convection (but Writeup says: not used...)

40. DLRK: Heat transfer due to differential rotation

41. Δ(enth): Difference in enthalpy between star 1 and 2

42. XIK

43. V^2: $\Delta\Phi_{surf}$ between star 1 and 2

44. FAC2 $\sim V^2$?

45. FAC1 $\sim V^2$?

46. Not used

47. Not used

48. Not used

49. Not used

50. RPP: Reaction rate: pp chain effective 2p $\rightarrow$ 1/2 He4

51. RPC: Reaction rate: effective C12 + 2 p $\rightarrow$ N14

52. RPNG: Reaction rate: effective N14 + 2p $\rightarrow$ O16

53. RPN: Reaction rate: effective N14 + 2p $\rightarrow$ C12 + He4

54. RPO: Reaction rate: effective O16 + 2p $\rightarrow$ N14 + He4

55. RAN: Reaction rate: effective N14 + 3/2 He4 $\rightarrow$ Ne20

56. $C_p dS/d \log p$

57. dL/dk

58. LQ, advection term for luminosity equation

59. ω, rotation rate

60. N^2: Brunt-Väisälä frequency squared **TODO: check this, the code suggests it's supposed to be the Richardson number, but this may be incorrect**

61. D_{dsi} mixing coefficient for the dynamical shear instability

62. D_{ssi} mixing coefficient for the secular shear instability

63. v_{ES} velocity of Eddington-Sweet circulation

64. v_μ counter term for Eddington-Sweet circultion ("μ-current")

65. $(4\pi r^2 \rho)^2/m'$, conversion factor for diffusion coefficients **CHECK**

66. **CHECK: SSSI? RIS?**

67. **TODO: ???**

68. **TODO: ???**

69. **CHECK:** $d\mu$?

70. **CHECK:** $d\omega$?

71. **CHECK: Convection + artificial mixing**

72. **CHECK: Thermohaline mixing**

73. **CHECK: Solberg-Hoiland mixing**

74. **CHECK: Dynamical-shear mixing**

75. **CHECK: Secular-shear mixing**

76. **CHECK: Eddington-Sweet mixing**

77. **CHECK: Goldberg-Schubert-Fricke mixing**

14 The independent variables

The independent variables are selected in `kp_var` in `init.dat` and are also known as `id(11:50)`, `ig(11:50)` in *e.g.* `solver()`. In *TWIN* mode, variables (25) to (40) are the same as (1) to (16), but for the companion star, while variables (17) to (24) are reserved for *binary* parameters.

(1/25) $\ln f$ - a dimensionless quantity closely related to electron degeneracy: for the case where electrons are non-degenerate and non-relativistic, $f \sim 10^8 \rho / T^{3/2}$

(2/26) $\ln T$ - logarithmic temperature (Kelvins)

(3/27) $X16$ - fractional abundance by mass of ^{16}O

(4/28) m - mass (10^{33} gm)

(5/29) $X1$ - the abundance of ^{1}H

(6/30) C - the gradient of mesh-spacing function $Q(f, T, m, r)$ with respect to mesh point number K. C does not vary with K, the mesh-point number, although it varies with time. It is in effect an eigenvalue

(7/31) $\ln r$ - logarithmic radius (10^{11} cm)

(8/32) L - luminosity (10^{33} erg/s). Not logged, because it may be negative

(9/33) $X4$ - the abundance of ^{4}He

(10/34) $X12$ - the abundance of ^{12}C

(11/35) $X20$ - the abundance of ^{20}Ne

For a more sophisticated binary, including mass loss, magnetic braking, rotation (uniform but time-varying) and tidal friction, a further 7 variables are stored:

(12/36) I - the moment of inertia of the interior material (10^{55} gm cm^2)

(13/37) $P_{\rm rot}$ - the rotation period (days) of the star (here taken to be independent of depth, so that it is an 'eigenvalue', like C above)

(14/38) ϕ - the centrifugal-gravitational potential (ergs).

(15/39) $\phi_{\rm s}$ - the potential at the surface, minus the potential on the L1 surface (ergs); an 'eigenvalue'.

(16/40) $X14$ - fractional abundance by mass of ^{14}N.

(17) $H_{\rm orb}$ - the orbital angular momentum (10^{50} gm cm^2/sec); an 'eigenvalue'.

(18) e - the eccentricity: an 'eigenvalue'.

(19) ξ - the flux of mass towards or away from the other star (formerly F) (10^{33} gm/sec); a function of depth, but zero below the L1 surface.

(20) $M_{\rm B}$ - the total mass of the binary; depleted by wind in either or both stars, but not by mass transfer between the stars. An 'eigenvalue'.

(22) Variable MENC for artificial, mesh-dependent energy term

(23) Variable MEA, related to MENC (Var. 22) and luminosity ...?

(24) Variable MET, related to MENC (Var. 22) ...?

(41) $X24$ - fractional abundance by mass of ^{24}Mg.

(42) $X28$ - fractional abundance by mass of ^{28}Si.

(43) $X56$ - fractional abundance by mass of ^{56}Fe.

(44) Total angular momentum.

15　The difference equations

The difference equations are selected in `kp_eqn` in `init.dat` and are also known as `id(51:90)`, `ig(51:90)` in *e.g.* `solver()`. See also the Writeup, Section 1.5 (p. 9) for more explanation.

(1 − 5, 13,14, 44,45) Abundance equations:
$$\sigma_{k+1/2}(X_{k+1}-X_k) - \sigma_{k-1/2}(X_k-X_{k-1}) = (\dot{X}_k+R_{\mathrm{nuc},k})m'_k - (X_{k+1}-X_k)[\dot{m}_k] + (X_k-X_{k-1})[-\dot{m}_{k+1}]$$

(1) ^{1}H abundance equation

(2) ^{16}O abundance equation

(3) ^{4}He abundance equation

(4) ^{12}C abundance equation

(5) ^{20}Ne abundance equation

(6) Pressure (rotation?) $\log P_{k+1} - \log P_k = -(Am')_{k+1/2}$

(7) Radius: $r_{k+1}^2 - r_k^2 = (m'/2\pi\rho r)_{k+1/2}$

(8) Temperature: $\log T_{k+1} - \log T_k = -(\nabla Am')_{k+1/2}$

(9) Luminosity: $L_{k+1} - L_k = (m'E_1)_{k+1/2} + (m'E_2)_k[\dot{m}_k] - (m'E_2)_{k+1}[-\dot{m}_{k+1}]$

(10) Mass: $m_{k+1}^{2/3} - m_k^{2/3} = (2m'/3m^{1/3})_{k+1/2}$

(11) Moment of inertia: $I_{k+1} - I_k = (2m'r^2/3)_{k+1/2}$

(12) Surface? L_1? potential: $\phi_{k+1} - \phi_k = (Gmm'/4\pi r^4\rho)_{k+1/2}$

(13) ^{14}N abundance equation

(14) ^{24}Mg abundance equation

(15) Sum of the abundances is constant: $\sum_i \dot{X}_i = 0$; normally used instead of (14) for ^{24}Mg.

(16) Equation for artificial, mesh-dependent energy term (MENC)

(18) Equation for MEA ...? — Related to MENC (Eq. 16) and luminosity ...?

(19) Mass-transfer rate: $\xi_{k+1} - \xi_k = \mathrm{CMT}\times(\sqrt{[2\phi_s]}/r\, m')_{k+1/2}$, if $\phi > 0$; $= 0$ otherwise.

(22) Equation for MET ...? — Related to MENC (Eq. 16) ...?

(25–37) CHECK ???

(42) Angular-momentum transport (...?)

(43) Total angular momentum (...?)

(44) ^{28}Si abundance equation

(45) ^{56}Fe abundance equation

16   The boundary conditions

The boundary conditions are selected in `kp_bc` in `init.dat` and are also known as `id(91:130)`, `ig(91:130)` in *e.g.* `solver()`.

16.1   Composition

(1a, 2a, 3a, 4a, 5a, 1b, 2b, 3b, 4b, 5b)

$$\sigma_{k\pm1/2}(X_k - X_{k\pm1}) = (\dot{X}_k + R_{\text{nuc},k}) \cdot (m_k - m_{k\pm1})$$

making 10 such equations in all.

16.2   At the surface (K = 1)

(6a) $dM/dt = -\,\text{CML} \cdot |\dot{M}_{\text{DDW}}(r, m, L, P_{\text{rot}})| - \text{CMJ} \cdot |\dot{M}_{\text{JNH}}| - \text{CMR} \cdot 1.3 \times 10^{-5} Lm/|E_B| - \text{CMS} \cdot [\ln(R/R_L)]^3$
$-\,\text{CMT} \cdot \xi + \text{CMI} \cdot M$

(7c) Pressure: $\frac{3}{2}P_{\text{gas}} + \frac{3}{4}P_{\text{rad}} \approx g/\kappa$

(8c) Luminosity/temperature: $L = \pi a c r^2 T^4$

(9c) $\phi = $ (gravitational) potential

(10c) $d(I\Omega)/dt = \ldots$, the rate of change of angular momentum of the star, carried away by stellar wind $|\dot{M}_{\text{DDW}}|$ or lost to the orbit by tidal friction ($\Omega \equiv 2\pi/P_{\text{rot}}$)

(11c) $\phi_s = \phi$: (gravitational) potential at the surface

(17c) $dH_{\text{orb}}/dt = \ldots$, rate of change of *orbital* angular momentum, including tidal friction which exchanges AM between spin and orbit

(18c) $de/dt = \ldots$, rate of circularisation due to tidal friction

(20c) $dM_B/dt = $ sum of the winds from both stars; M_B is the *binary* mass

16.3   At the centre (K = KH)

(actually one mesh point from the centre)

(6d) $m = 0$

(7d) $L = 0$

(8d) $r = 0$

(9d) $I = 0$

(19d) $\xi = 0$

(13) **CHECK ???**

(20) **CHECK ???**

(25–29) **CHECK ???**

(30–33) **CHECK ???** (2x)

(34) **CHECK ???**

(35) **CHECK ???**

(37) **CHECK ???**